

Loesung zu H31a:

```
n_1 = 5
n_2 = 10
n_3 = 3
n_4 = 12
n_5 = 5
n_6 = 50
n_7 = 6

m_[1][2]=min{m[1][1]+m[2][2]+n_{0}n_{1}n_{2}}=min{0+0+5*10*3}=
=min{150}=150
s[1][2]=1

m_[2][3]=min{m[2][2]+m[3][3]+n_{1}n_{2}n_{3}}=min{0+0+10*3*12}=
=min{360}=360
s[2][3]=2

m_[3][4]=min{m[3][3]+m[4][4]+n_{2}n_{3}n_{4}}=min{0+0+3*12*5}=
=min{180}=180
s[3][4]=3

m_[4][5]=min{m[4][4]+m[5][5]+n_{3}n_{4}n_{5}}=min{0+0+12*5*50}=
=min{3000}=3000
s[4][5]=4

m_[5][6]=min{m[5][5]+m[6][6]+n_{4}n_{5}n_{6}}=min{0+0+5*50*6}=
=min{1500}=1500
s[5][6]=5

m_[1][3]=min{m[1][1]+m[2][3]+n_{0}n_{1}n_{3}}, m[1][2]+m[3][3]+n_{0}n_{2}n_{3}}=
=min{0+360+5*10*12, 150+0+5*3*12}=min{960, 330}=330
s[1][3]=2

m_[2][4]=min{m[2][2]+m[3][4]+n_{1}n_{2}n_{4}}, m[2][3]+m[4][4]+n_{1}n_{3}n_{4}}=
=min{0+180+10*3*5, 360+0+10*12*5}=min{330, 960}=330
s[2][4]=2

m_[3][5]=min{m[3][3]+m[4][5]+n_{2}n_{3}n_{5}}, m[3][4]+m[5][5]+n_{2}n_{4}n_{5}}=min{0+3000+3*12*50, 180+0+3*5*50}=
=min{4800, 930}=930
s[3][5]=4

m_[4][6]=min{m[4][4]+m[5][6]+n_{3}n_{4}n_{6}}, m[4][5]+m[6][6]+n_{3}n_{5}n_{6}}=min{0+1500+12*5*6, 3000+0+12*50*6}=
=min{1860, 6600}=1860
s[4][6]=4

m_[1][4]=min{m[1][1]+m[2][4]+n_{0}n_{1}n_{4}}, m[1][2]+m[3][4]+n_{0}n_{2}n_{4}}, m[1][3]+m[4][4]+n_{0}n_{3}n_{4}}=
=min{0+330+5*10*5, 150+180+5*3*5, 330+0+5*12*5}=
=min{580, 405, 630}=405
s[1][4]=2

m_[2][5]=min{m[2][2]+m[3][5]+n_{1}n_{2}n_{5}}, m[2][3]+m[4][5]+n_{1}n_{3}n_{5}}, m[2][4]+m[5][5]+n_{1}n_{4}n_{5}}=
=min{0+930+10*3*50, 360+3000+10*12*50, 330+0+10*5*50}=min{2430, 9360, 2830}=2430
s[2][5]=2

m_[3][6]=min{m[3][3]+m[4][6]+n_{2}n_{3}n_{6}}, m[3][4]+m[5][6]+n_{2}n_{4}n_{6}},
m[3][5]+m[6][6]+n_{2}n_{5}n_{6}}=
=min{0+1860+3*12*6, 180+1500+3*5*6, 930+0+3*50*6}=min{2076, 1770, 1830}=1770
s[3][6]=4

m_[1][5]=min{m[1][1]+m[2][5]+n_{0}n_{1}n_{5}}, m[1][2]+m[3][5]+n_{0}n_{2}n_{5}}, m[1][3]+m[4][5]+n_{0}n_{3}n_{5}},
m[1][4]+m[5][5]+n_{0}n_{4}n_{5}}=
=min{0+2430+5*10*50, 150+930+5*3*50, 330+3000+5*12*50, 405+0+5*5*50}=min{4930, 1830, 6330, 1655}=1655
s[1][5]=4

m_[2][6]=min{m[2][2]+m[3][6]+n_{1}n_{2}n_{6}}, m[2][3]+m[4][6]+n_{1}n_{3}n_{6}}, m[2][4]+m[5][6]+n_{1}n_{4}n_{6}},
m[2][5]+m[6][6]+n_{1}n_{5}n_{6}}=min{0+1770+10*3*6, 360+1860+10*12*6, 330+1500+10*5*6, 2430+0+10*50*6}=
=min{1950, 2940, 2130, 5430}=1950
s[2][6]=2

m_[1][6]=min{m[1][1]+m[2][6]+n_{0}n_{1}n_{6}}, m[1][2]+m[3][6]+n_{0}n_{2}n_{6}}, m[1][3]+m[4][6]+n_{0}n_{3}n_{6}},
m[1][4]+m[5][6]+n_{0}n_{4}n_{6}}, m[1][5]+m[6][6]+n_{0}n_{5}n_{6}}=
=min{0+1950+5*10*6, 150+1770+5*3*6, 330+1860+5*12*6, 405+1500+5*5*6, 1655+0+5*50*6}=
=min{2250, 2010, 2550, 2055, 3155}=2010
s[1][6]=2
```

Die optimale Klammerung ist also ((A_1A_2) ((A_3A_4) (A_5A_6))).

Loesung zu H-31b:

C	G	C	G	T	A	C	T
+0	+0	+0	+0	+0	+0	+0	+0
G	+0	^0	\1	<1	\1	<1	<1
T	+0	^0	^1	^1	^1	\2	<2
A	+0	^0	^1	^1	^1	^2	\3
C	+0	\1	^1	\2	<2	^2	^3
C	+0	\1	^1	\2	^2	^2	\4
A	+0	^1	^1	^2	^2	\3	^4
T	+0	^1	^1	^2	^2	\3	^4
G	+0	^1	\2	^2	\3	^3	^4
T	+0	^1	\2	^2	\3	\4	\5

GTACT (length 5)